

More practices on radicals
Precalculus RH

10. (47%) If $a < b$, find the ordered pair of positive integers (a,b) that satisfies

$$\sqrt{10 + \sqrt{84}} = \sqrt{a} + \sqrt{b} .$$

16. (39%) If $a > 0$, $b > 0$, $a \neq b$, and $\frac{a\sqrt{b} + b\sqrt{a}}{a\sqrt{b} - b\sqrt{a}} - \frac{a\sqrt{b} - b\sqrt{a}}{a\sqrt{b} + b\sqrt{a}} = \sqrt{ab}$, write an equation expressing a explicitly in terms of b .

22. (32%) Find all ordered triples of real numbers (x,y,z) that satisfy

$$\begin{cases} \sqrt{x - y + z} = \sqrt{x} - \sqrt{y} + \sqrt{z}, \\ x + y + z = 8, \text{ and} \\ x - y + z = 4. \end{cases}$$

25. The expression $\sqrt{10 + \sqrt{10 + \sqrt{10 + \dots}}}$, where the dots indicate an infinite repetition of the indicated pattern of operations, can be expressed in the form $\frac{a + \sqrt{b}}{c}$, where a , b , and c are integers, no two of which have a common prime factor. Find the ordered triple (a,b,c) .

26. (25%) If $a = \sqrt{.16}$, $b = \sqrt[3]{.0639}$, $c = \sqrt[6]{.0041}$, and $d = (.2)^2$, arrange a , b , c , and d in increasing order.