

Show your work for full credits.

Part I – Calculator (6 pts each)

1. If  $\ln a = 2.11$ , what is the value of  $\ln(ae^2)$ ?

2. Let  $3.12^a = 2.13^b$ . what is the value of  $\frac{a}{b}$ ?

3. In  $\triangle ABC$ ,  $AB = 10$ ,  $BC = 10$ ,  $m\angle B = 40^\circ$ . Find  $AC$ .

Part II – No Calculator (10 pts each)

Name: \_\_\_\_\_

4. Prove

*\*you may work on only one side of the equation.*

$$\frac{\tan a + \tan b}{\cot a + \cot b} = (\tan a)(\tan b)$$

5. Simplify the given expression in terms of  $A$ .

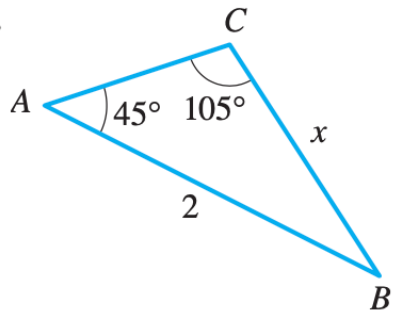
$$\frac{1}{x^2\sqrt{9+x^2}}, \quad x = 3 \tan A$$

6. Let  $n = \log_2 3 \cdot \log_3 4 \cdot \log_4 5 \cdots \log_{2019} 2020$ . What is the least integer greater than  $n$ ?

7. What is the value of the given summation?

$$\sum_{i=1}^{10} \sum_{j=1}^{10} (ij)$$

8. Find the value of  $x$ . Then, find the area of the triangle.



9. Write the first expression in terms of the second, for  $A$  in the given quadrant.

$\csc^2 A \cos^2 A,$        $\sin A;$        $A$  in any quadrant

10. Find the exact value of the given expressions.

a.  $\tan(-240^\circ)$

b.  $\sec \frac{16\pi}{3}$

11. A point  $P$  moving in simple harmonic motion completes 8 cycles every second. If the amplitude of the motion is 40 cm, find an equation that describes the motion of  $P$  as a function of time. Assume the point  $P$  is at its maximum displacement when  $t = 0$ .