Show your work for full credits.

1. $f(x)=\frac{a x-4}{b x+6}$ has vertical asymptote at $x=-2$ and horizontal asymptote at $y=\frac{3}{2}$. Then, find the value of $a+b$.
2. Let $y=\frac{2 x^{2}-7 x+9}{2 x-3}$
a. State any asymptotes.
b. Find x and y intercepts.
c. Sketch the given function.

3. From the given graph below,
a. Find asymptotes.
b. Find $x$ and $y$-intercepts
c. Write an equation for the function below.

4. Let $P(x)$ be a polynomial which when divided by $x-20$ has the remainder 19 , and when divided by $x-19$ has the remainder 20. What is the remainder when $P(x)$ is divided by $(x-19)(x-20)$ ?
5. Suppose that $P(2 x)=x^{2}+3 x-1$. What is the product of all values of $x$ for which $P\left(\frac{x}{4}\right)=5$ ?
6. Divide, using synthetic division. Then, express the given fraction by quotient and remainder.
a. $\frac{3 x^{3}+x^{2}-10 x+5}{(x-1)(x+2)}$
b. $\frac{6 x^{2}-x-6}{2 x-1}$
7. Evaluate
a. $\arccos \left(\cos \frac{4 \pi}{3}\right)$
b. $\arctan \left(\tan \frac{11 \pi}{6}\right)$
8. Let $h(x)=f(g(x))=\sqrt{2 x-1}$. If $f(x)=(x-3)^{2}+2$, find $g(x)$.
9. Let $f(x)=x+\sqrt{x-3}$ and $g(f(x))=x$. Find the solution for $f(x)=g(x)$
