

5. Suppose that  $a$  and  $b$  are integers such that  $x^2 - x - 1$  is a factor of  $ax^3 + bx^2 + 1$ . What is  $b$ ?
- a) -2    b) -1    c) 0    d) 1    e) 2

$$ax^3 + bx^2 + 1 = (x^2 - x - 1)(ax - 1)$$

$$bx^2 = -x^2 - ax^2 = -2x^2 \rightarrow b = -2$$

$$0x = x - ax \rightarrow a = 1$$

$$|x| = \sqrt{x^2}$$

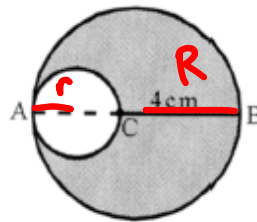
$$\text{ex) } \sqrt{x^2 - 4x + 4} = \sqrt{(x-2)^2} = |x-2|$$

$$\sqrt{x^6} = |x^3|$$

$$\frac{6(\sqrt{4} + \sqrt{2} + 1)}{(\sqrt{2} - 1)(\sqrt{4} + \sqrt{2} + 1)} \frac{(a-b)(a^2 + ab + b^2)}{(a-b)(a^2 + ab + b^2)}$$

$$= \frac{6(\sqrt{4} + \sqrt{2} + 1)}{2 - 1} = 6(\sqrt{4} + \sqrt{2} + 1)$$

- 1.521 Two circles are internally tangent at A, with diameter AB intersecting the smaller circle at C. The shaded region has an area of  $9\pi \text{ cm}^2$ , and  $BC = 4 \text{ cm}$ . What is the sum of the radii of the two circles?



$$\pi R^2 - \pi r^2 = 9\pi$$

$$R^2 - r^2 = 9$$

$$(R+r)(R-r) = 9$$

$$2R - 2r = 4$$

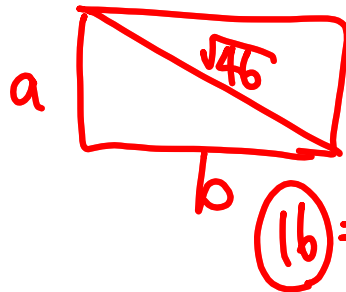
$$R - r = 2$$

$$R + r = ?$$

$$= \left(\frac{9}{2}\right)$$

1.621 The diagonal length of a rectangle is  $\sqrt{46}$ , and its area is  $9\text{cm}^2$ . Find its perimeter. (See section 5.3).

$$A=9$$



$$\left. \begin{array}{l} a^2 + b^2 = 46 \\ ab = 9 \end{array} \right\} (a+b)^2$$

$$= a^2 + 2ab + b^2$$

$$= 46 + 18$$

$$= 64$$

$$2(a+b) = 64$$

1.721 The sum of two positive numbers is 6, and the sum of their squares is 22. What is the sum of their reciprocals? Express your answer as a common fraction.

$$a^2 + b^2 + 2ab = 36$$

$$(a+b)^2 = 36$$

$$a^2 + b^2 = 22$$

$$2ab = 14$$

$$\frac{1}{a} + \frac{1}{b} = \frac{a+b}{ab}$$

$$= \frac{6}{7}$$

$$\begin{array}{l}
 \begin{array}{l}
 \text{25)} \\
 \curvearrowright (2x+1)(x+1) \\
 2x^2 + 3x + 1
 \end{array} \\
 \hline
 \begin{array}{l}
 \curvearrowleft x^2 + 2x - 15 \\
 (x+5)(x-3)
 \end{array}
 \end{array}
 \div
 \begin{array}{l}
 \begin{array}{l}
 (x+5)(x+1) \\
 x^2 + 6x + 5
 \end{array} \\
 \hline
 \begin{array}{l}
 \curvearrowleft 2x^2 - 7x + 3 \\
 (2x-1)(x-3)
 \end{array}
 \end{array}
 \quad x \neq \frac{1}{2}, 3$$

$$\frac{\cancel{(2x+1)}\cancel{(x+1)}}{\cancel{(x+5)}\cancel{(x-3)}} \cdot \frac{\cancel{(2x-1)}\cancel{(x-3)}}{\cancel{(x+5)}\cancel{(x+1)}} = \frac{(2x+1)(2x-1)}{(x+5)^2}$$

$$\frac{\left(\frac{2}{x} - \frac{1}{y}\right) xy^2}{\left(\frac{1}{xy^2}\right) xy^2} \quad \frac{1y}{xy} + \frac{1}{xy} =$$