

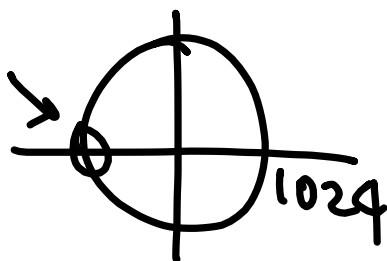
$$65. (1 + i)^{20}$$

$$= (\sqrt{2} \operatorname{cis} 45^\circ)^{20}$$

$$= 1024 \operatorname{cis} 900^\circ$$

$$= 1024 \operatorname{cis} 180^\circ$$

$$= -1024$$



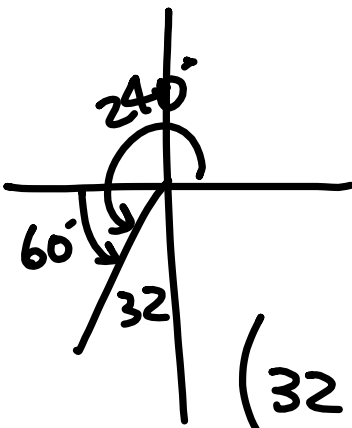
$$(r_1 \operatorname{cis} \theta_1)(r_2 \operatorname{cis} \theta_2)$$

$$= r_1 r_2 \operatorname{cis}(\theta_1 + \theta_2)$$

$$r \operatorname{cis} \theta = r e^{\theta i}$$

$$(r e^{\theta i})^n = r^n e^{n \theta i} = r^n \operatorname{cis} n \theta$$

86. The fifth roots of  $-16 - 16\sqrt{3}i$



$$(32 \operatorname{cis} 240^\circ)^{\frac{1}{5}}$$

$$\begin{aligned} & (r \operatorname{cis} \theta)^{\frac{1}{n}} \\ &= r^{\frac{1}{n}} \operatorname{cis} \left( \frac{\theta}{n} + \frac{2\pi k}{n} \right) \end{aligned}$$

①  $2 \operatorname{cis} 48^\circ$

②  $2 \operatorname{cis} 120^\circ$

$2 \operatorname{cis} 192^\circ$

$2 \operatorname{cis} 264^\circ$

$2 \operatorname{cis} 336^\circ$

$$89. z^3 - 4\sqrt{3} - 4i = 0$$

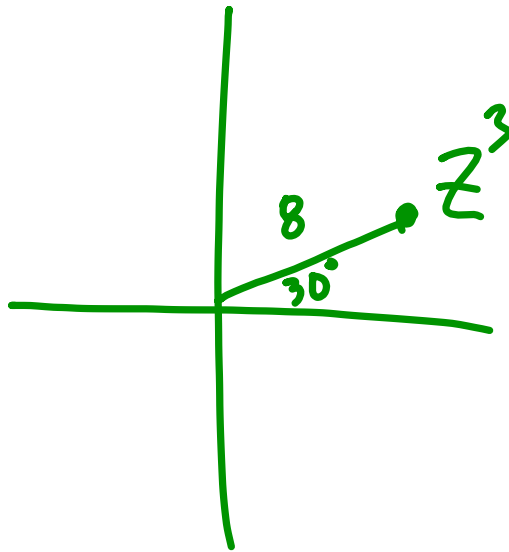
$$z^3 = 4\sqrt{3} + 4i$$

$$z = \sqrt[3]{4\sqrt{3} + 4i}$$

$$z_1 = 2 \operatorname{cis} 10^\circ$$

$$z_2 = 2 \operatorname{cis} 130^\circ$$

$$\begin{aligned} z_3 &= 2 \operatorname{cis} 250^\circ = 2 \cos 250^\circ + 2i \sin 250^\circ \\ &= -.68 - 1.88i \end{aligned}$$



93. (a) Let  $w = \cos \frac{2\pi}{n} + i \sin \frac{2\pi}{n}$  where  $n$  is a positive integer. Show that  $1, w, w^2, w^3, \dots, w^{n-1}$  are the  $n$  distinct  $n$ th roots of 1.

(b) If  $z \neq 0$  is any complex number and  $s^n = z$ , show that the  $n$  distinct  $n$ th roots of  $z$  are

$$s, sw, sw^2, sw^3, \dots, sw^{n-1}$$

$n^{\text{th}}$  root of 1 =  $\sqrt[n]{1} = \sqrt[n]{|1|e^{i0}}$

