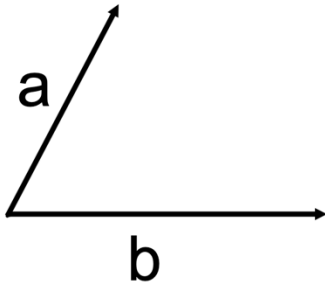


Show your work for full credits. (#1 to 5: 95 pts / #6: 10 pts)

1. Two vectors as shown below have  $|a| = 3$ ,  $|b| = 5$ , and angle between them is  $60^\circ$ .



- $a \cdot b$
- $|a \times b|$
- What is the direction of  $a \times b$ ?
- $a \times a$
- $a \cdot a$
- $\text{comp}_b a$

2. Given the points  $A(0, 0, 0)$ ,  $B(1, 4, 0)$ ,  $C(2, 0, 5)$ , and  $D(0, 1, 6)$ , where  $B$ ,  $C$ , and  $D$  are neighboring vertices of  $A$  in parallelepiped.
- Find the volume of the parallelepiped
  - Find the surface area of the parallelepiped

3. Find the acute angle between two diagonals of a cube.

4. Find the distance from the origin to the line

$$x = 2 - t, \quad y = 1 + 2t, \quad z = -2 + t$$

5. Determine whether the lines given are parallel, skew, or intersecting.

If parallel, find the distance between the lines, if intersecting, find the point of intersection.

$$\begin{aligned} x &= 2 - t, & y &= 1 + 2t, & z &= -2 + t \\ x &= 2t, & y &= 8 - t, & z &= 5 + 3t \end{aligned}$$

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6. Let  $B$  be a solid box with length  $L$ , width  $W$ , and height  $H$ . Let  $S$  be the set of all points that are a distance at most 1 from some point of  $B$ . Express the volume of  $S$  in terms of  $L$ ,  $W$ , and  $H$ .