

Let $f(x, y) = 2xy + y^2$ * partial deriv.

$$\lim_{h \rightarrow 0} \frac{f(x+h, y) - f(x, y)}{h} = \frac{\partial f}{\partial x}$$

$$= \lim_{h \rightarrow 0} \frac{\overbrace{2(x+h)y + 2hy}^{2xy + 2hy} + \cancel{y^2} - (\cancel{2xy} + \cancel{y^2})}{h} = 2y$$

$$\text{Let } f(x, y) = 2xy + y^2$$

$$\lim_{h \rightarrow 0} \frac{f(x, y+h) - f(x, y)}{h} = 2x + 2y$$

$$z = xy - \sin(x^2 + y) - e^{\sqrt{x}y}$$

$$\frac{\partial z}{\partial x} = y - \cos(x^2 + y)2x - \frac{y}{2\sqrt{x}}e^{\sqrt{x}y}$$

$$\frac{\partial z}{\partial y} = x - \cos(x^2 + y) - \sqrt{x}e^{\sqrt{x}y}$$

$$f(x,y) = 2x^2y - e^{xy} \quad \frac{d}{dx} = -ye^{xy}$$

$$\frac{d}{dx} \left(\frac{df}{dx} \right) = \frac{d^2f}{dx^2} = 4y - y^2e^{xy}$$

$$\frac{d}{dy} = -e^{xy} - xy e^{xy}$$

$$\frac{d^2f}{dy^2} = -x^2e^{xy}$$

$$\frac{d}{dy} \left(\frac{df}{dx} \right) = \frac{d^2f}{dydx} = 4x - xy e^{xy}$$

$$\frac{d^2f}{dx dy} =$$