## AP review

## Volumes 2

2013

5. Let $f(x)=2 x^{2}-6 x+4$ and $g(x)=4 \cos \left(\frac{1}{4} \pi x\right)$. Let $R$ be the region bounded by the graphs of $f$ and $g$, as shown in the figure above.
(a) Find the area of $R$.
(b) Write, but do not evaluate, an integral expression that gives the volume of the solid generated when $R$ is rotated about the horizontal line $y=4$.
(c) The region $R$ is the base of a solid. For this solid, each cross section perpendicular to the $x$-axis is a square. Write, but do not evaluate, an integral expression that gives the volume of the solid.

## 2014 (calculator)


2. Let $R$ be the region enclosed by the graph of $f(x)=x^{4}-2.3 x^{3}+4$ and the horizontal line $y=4$, as shown in the figure above.
(a) Find the volume of the solid generated when $R$ is rotated about the horizontal line $y=-2$.
(b) Region $R$ is the base of a solid. For this solid, each cross section perpendicular to the $x$-axis is an isosceles right triangle with a leg in $R$. Find the volume of the solid.
(c) The vertical line $x=k$ divides $R$ into two regions with equal areas. Write, but do not solve, an equation involving integral expressions whose solution gives the value $k$.

