

3. Each side of a square is increasing at a rate of  $6 \text{ cm/s}$ . At what rate is the area of the square increasing when the area of the square is  $16 \text{ cm}^2$ ?

$$\frac{ds}{dt} = +6 \text{ cm/s}$$

$$A = s^2 = 16 \text{ cm}^2$$

$$\hookrightarrow s = 4 \text{ cm}$$

$$\frac{dA}{dt} = ?$$

$$A = s^2$$

$$\frac{dA}{dt} = 2s \frac{ds}{dt}$$

$$= 2(4)6$$

$$= 48 \text{ cm}^2/\text{s}$$

5. A cylindrical tank with radius 5 m is being filled with water at a rate of  $3 \text{ m}^3/\text{min}$ . How fast is the height of the water increasing?

$$V = \pi r^2 h$$

$$V = 25\pi h$$

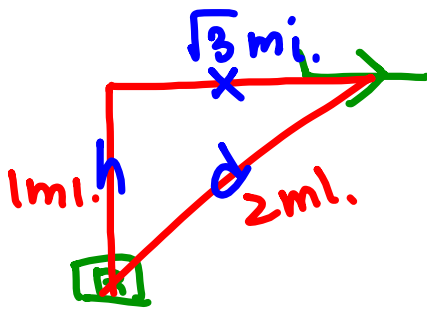
$$\frac{dV}{dt} = 25\pi \frac{dh}{dt}$$

$$3 = 25\pi \frac{dh}{dt}$$

$$\frac{dh}{dt} = \frac{3}{25\pi} \text{ m/min}$$

$$\frac{dV}{dt} = 3 \text{ m}^3/\text{min}$$

- (a) What quantities are given in the problem?  
 (b) What is the unknown?  
 (c) Draw a picture of the situation for any time  $t$ .  
 (d) Write an equation that relates the quantities.  
 (e) Finish solving the problem.
11. A plane flying horizontally at an altitude of 1 mi and a speed of 500 m/h passes directly over a radar station. Find the rate at which the distance from the plane to the station is increasing when it is 2 mi away from the station.



$$h^2 + x^2 = d^2$$

$$\rightarrow l^2 + x^2 = d^2$$

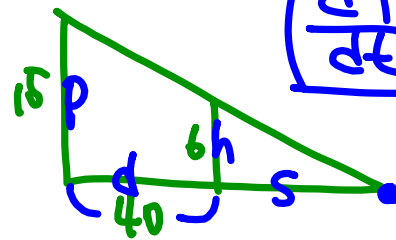
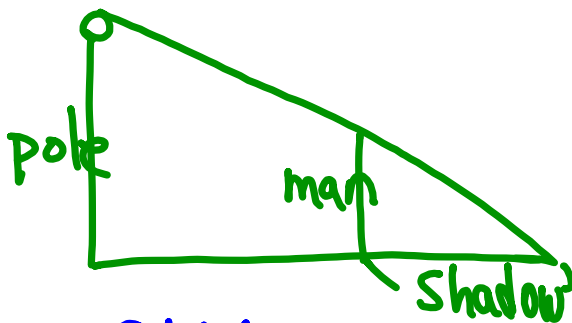
$$2x \frac{dx}{dt} = 2d \frac{dd}{dt}$$

$$\sqrt{3}(500) = 2 \frac{dd}{dt}$$

$$\frac{dd}{dt} = 250\sqrt{3} \text{ m/h}$$

13. A street light is mounted at the top of a 15-ft-tall pole. A man 6 ft tall walks away from the pole with a speed of 5 ft/s along a straight path. How fast is the tip of his shadow moving when he is 40 ft from the pole?

\* similar  $\Delta$



$$\frac{dT}{dt} = \frac{dd}{dt} + \frac{ds}{dt}$$

$$6d + 6s = 15s$$

$$6d = 9s$$

$$\frac{6}{s} = \frac{15}{ds}$$

$$6 \frac{dd}{dt} = 9 \frac{ds}{dt}$$

$$6(5) = 9 \frac{ds}{dt}$$

$$\frac{30}{9} = \frac{ds}{dt}$$

$$\frac{dT}{dt} = 5 + \frac{10}{3}$$

$$= \frac{25}{3} \frac{\text{ft}}{\text{s}}$$