

**Example 1 (numerical).**

The data in the table below give selected values for the velocity, in meters/minute, of a particle moving along the  $x$ -axis. The velocity  $v$  is a differentiable function of time  $t$ .

Time $t$ (min)	0	2	5	6	8	12
Velocity $v(t)$ (meters/min)	-3	2	3	5	7	5

Avg acc.

$$\frac{5}{2}$$

$$\frac{1}{3}$$

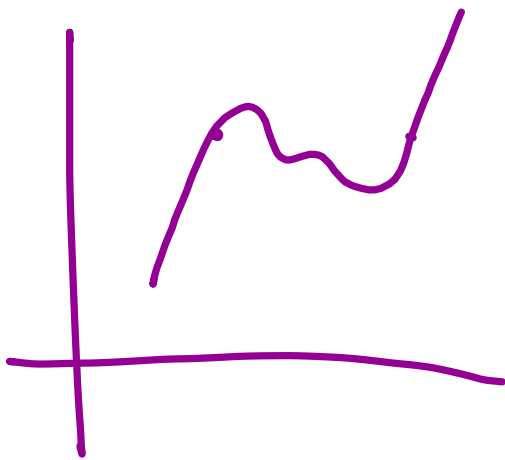
$$2$$

$$1$$

$$-\frac{1}{2}$$

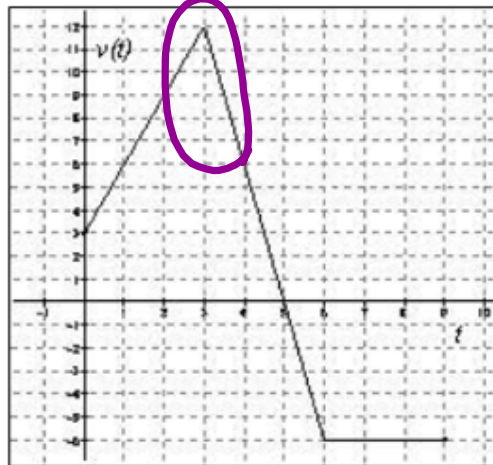
4. Let  $a(t)$  denote the acceleration of the particle at time  $t$ . Is there guaranteed to be a time  $t = c$  in the interval  $0 \leq t \leq 12$  such that  $a(c) = 0$ ? Justify your answer.

Since Avg accl. for  $[6, 8]$  was  $1 \text{ m/min}^2$  & for  $[8, 12]$  was  $-\frac{1}{2} \text{ m/min}^2$ , there must be time  $t = c$ , where  $a(c) = 0$



**Example 2 (graphical).**

The graph below represents the velocity  $v$ , in feet per second, of a particle moving along the  $x$ -axis over the time interval from  $t = 0$  to  $t = 9$  seconds.



$$[2, 3]$$

$$v' = 3$$

$$[3, 4]$$

$$v' = -6 \therefore v' \neq -\frac{3}{2}$$

5. Is there guaranteed to be a time  $t$  in the interval  $2 \leq t \leq 4$  such that  $v'(t) = -3/2$  ft/sec<sup>2</sup>? Justify your answer.

1. A particle moves along the  $x$ -axis so that its position at time  $t$  is given by  $x(t) = t^2 - 6t + 5$ . For what value of  $t$  is the velocity of the particle zero?

(A) 1

(B) 2

(C) 3

(D) 4

(E) 5

$$x' = v = 2t - 6 = 0$$

$$t = 3$$

4. A particle moves along the y-axis so that its position at any time  $t$ , for  $0 \leq t \leq 5$ , is given by  $y(t) = t^4 - 18t^2$ .

In which interval(s) is the particle speeding up?

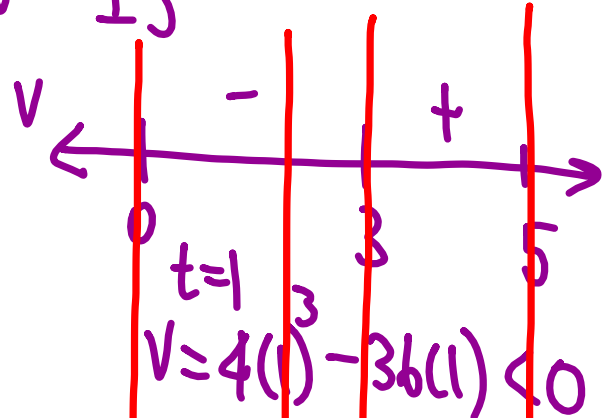
- (A)  $0 < t < \sqrt{3}$   
 (B)  $0 < t < \sqrt{3}$  and  $3 < t < 5$   
 (C)  $3 < t < 5$   
 (D)  $\sqrt{3} < t < 3$  and  $3 < t < 5$   
 (E)  $\sqrt{3} < t < 3$

①  $v$  &  $a$  have the same sign.

②  $v(t) = y'$  is moving away from  $t$ -axis.

$$y' = 4t^3 - 36t \rightarrow 4t(t^2 - 9) = 0$$

$$\begin{array}{c} \downarrow \quad \downarrow \\ 0 \quad \pm 3 \end{array}$$



$$y'' = 12t^2 - 36$$

$$\rightarrow 12(t^2 - 3) = 0$$

$$\downarrow$$

$$t = \pm\sqrt{3}$$

Speed up  
 $[0, \sqrt{3}]$  or  $[3, 5]$

