

$$11. g(t) = \frac{1}{(t^4 + 1)^3} \quad g' = -3(t^4 + 1)^{-4} (4t^3)$$

$$f = (t^4 + 1)^{-3}$$

$$g(u) = u^{-3}$$

$$u = t^4 + 1$$

$$g' = \frac{dg}{du} \cdot \frac{du}{dx}$$

$$g' = \frac{-3(4t^3)}{(t^4 + 1)^4}$$

$$15. y = xe^{-kx}$$

$$= (x)(e^{-kx})$$

$$(zx)' = z$$

$$(-kx)' = -k$$

$$\frac{dy}{dx} = (x)'e^{-kx} + (e^{-kx})'(x)$$

$$= 1 \cdot e^{-kx} + e^{-kx}(-k)x$$

$$\frac{dy}{dx} = e^{-kx} - kxe^{-kx}$$

$$17. g(x) = (1 + 4x)^5(3 + x - x^2)^8$$

$$\begin{aligned} g' &= \left((1+4x)^5 \right)' (3+x-x^2)^8 + \left((3+x-x^2)^8 \right)' (1+4x)^5 \\ &= 5(1+4x)^4 \cdot 4(3+x-x^2)^8 + 8(3+x-x^2)^7(1-2x)(1+4x)^5 \\ &= 4(1+4x)^4 (3+x-x^2)^7 \left(5(3+x-x^2) + 2(1-2x)(1+4x) \right) \\ &= 4(1+4x)^4 (3+x-x^2)^7 (-21x^2 + 9x + 17) \end{aligned}$$

$$19. y = (2x - 5)^4(8x^2 - 5)^{-3}$$

$$\begin{aligned} y' &= \left((2x-5)^4 \right)' (8x^2-5)^{-3} + \left((8x^2-5)^{-3} \right)' (2x-5)^4 \\ &= 4(2x-5)^3 \cdot 2(8x^2-5)^{-3} - 3(8x^2-5)^{-4} (16x) (2x-5)^4 \end{aligned}$$

if $x=0$

$$= 4(-5)^3 \cdot 2(-5)^{-3} - 3(-5)^{-4} \cdot 0 \approx$$

$$= 8$$