

If $f'(x) = 2x$, Find $f(x)$.

$$f(x) = x^2 + C$$

Let $f'(x) = \sqrt{x}$, Find $f(x)$.

$$= x^{\frac{1}{2}}$$
$$\frac{2}{3}x^{\frac{3}{2}} + c = f(x)$$

Reverse power rule

$$f'(x) = x^n, \quad f(x) = \frac{1}{n+1} x^{n+1} + C$$

$$6. \int (\sqrt{x^3} + \sqrt[3]{x^2}) dx = \int x^{\frac{3}{2}} + x^{\frac{2}{3}} dx$$

\uparrow

$$f'(x) = \frac{2}{5}x^{\frac{5}{2}} + \frac{3}{5}x^{\frac{5}{3}} + C$$

$$8. \int (y^3 + 1.8y^2 - 2.4y) dy =$$

$$f'(x) = y^3 + 1.8y^2 - 2.4y$$

$$f(x) = \left[\frac{1}{4}y^4 + \frac{1}{3}(1.8)y^3 - \frac{1}{2}(2.4)y^2 \right]$$
$$\boxed{\frac{1}{4}y^4 + 0.6y^3 - 1.2y^2 + C}$$

$$10. \int v(v^2 + 2)^2 dv = \frac{v^6}{6} + V^4 + 2V^2 + C$$

$$\begin{aligned}& (v^2+2)(v^2+2) \\& \checkmark (v^4 + 4v^2 + 4)\end{aligned}$$

$$\checkmark v^5 + 4v^3 + 4v$$

$$f(x) = \frac{1}{6}v^6 + \frac{1}{4}(4v)^4 + \frac{1}{2}(4v)^2 + C$$

$$f(x) = \frac{1}{6}v^6 + v^4 + 2v^2 + C$$

$$12. \int \left(x^2 + 1 + \frac{1}{x^2 + 1} \right) dx$$

$$= \frac{1}{3}x^3 + x + \arctan x + C$$

$$14. \int (\csc^2 t - 2e^t) dt$$

$$f(x) = -\cot(t) - e^t + C$$

16. $\int \sec t (\sec t + \tan t) dt$